

# Hybrid Automata

Simulated



# Definition

- Formal model of a hybrid system.
- Transition system that is extended with continuous dynamics

# Tuple

– A hybrid automaton  $H$  is a tuple  $H = (Q, V, f, \text{Init}, \text{Inv}, \Theta, G, R, \Sigma, \lambda)$ ,

- $Q = \{q_1, \dots, q_k\}$  is a finite set of discrete states (control locations);

- $\Theta \subseteq Q \times Q$  is the transition relation;

- $G: \Theta \rightarrow 2^{R^n}$  is the guard condition;

- $V = \{x_1, \dots, x_m\}$  is a finite set of continuous variables;

- $f: Q \times R^n \rightarrow R^n$  is an activity function;

- $\text{Inv}: Q \rightarrow 2^{R^n}$  describe the invariants of the locations;

- $R: \Theta \rightarrow 2^{R^n} \times 2^{R^n}$  is the reset map;

- $\text{Init} \subset Q \times R^n$  is the set of initial states;

- $\Sigma$  is a finite set of synchronization labels;  $\lambda: \Theta \rightarrow \Sigma$  is the labeling function.

Specifies  
discrete  
dynamics

Describes  
continuous  
dynamics & its  
limitations

Necessary to  
synchronize  
different systems.

# Thermostat (Model & Simulation)

$$f(q, x) := \begin{cases} -x + 50 & q = \text{off} \\ -x + 100 & q = \text{on} \end{cases} \quad \varphi(q, x) := \begin{cases} \text{on}, & q = \text{off}, x \leq 73 \\ \text{off}, & q = \text{off}, x > 73 \\ \text{off}, & q = \text{on}, x \geq 77 \\ \text{on}, & q = \text{on}, x < 77 \end{cases}$$



# Scilab vs Uppaal

## Scilab

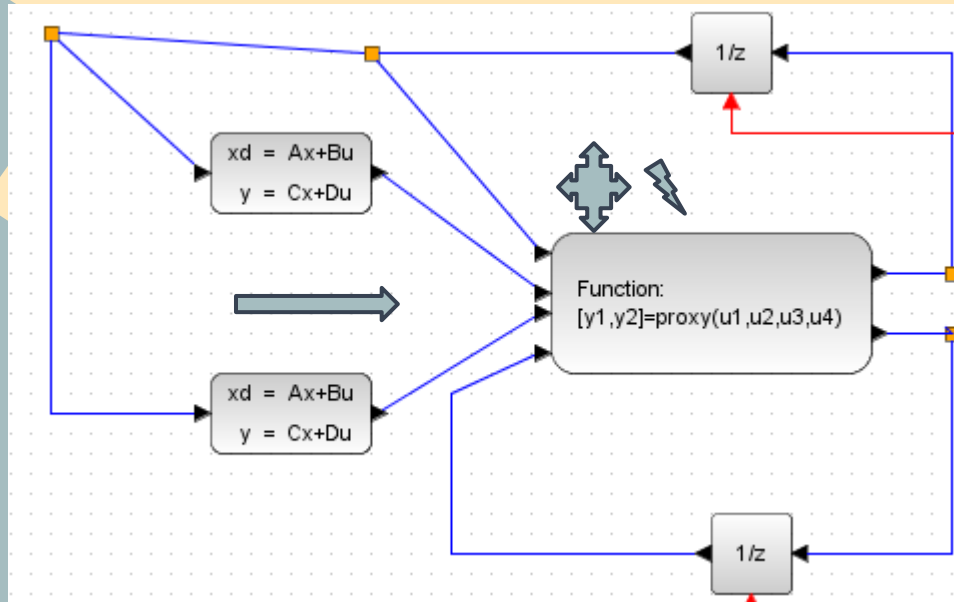
- Continuous
- Numeric Graph
- Visual Output
- Simulation

## Uppaal

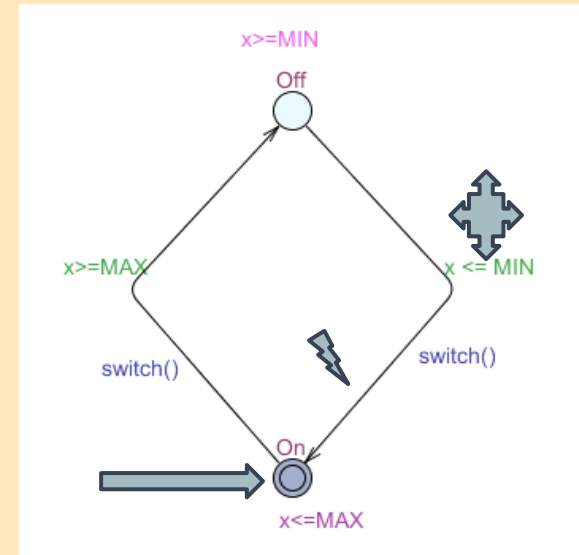
- Discrete
- Directed Graph
- Traced Query
- Verification

# Discrete Dynamics

## Scilab

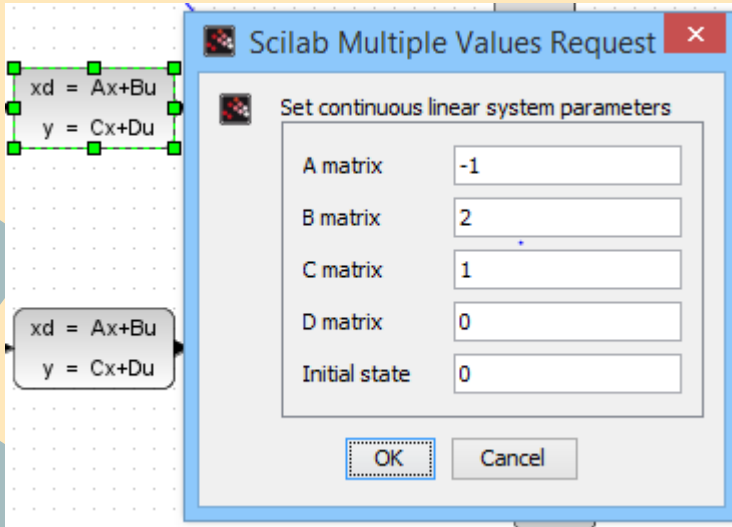


## Uppaal



# Continuous Dynamics

Scilab

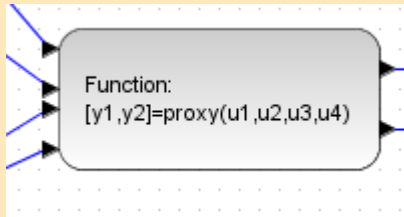


Uppaal

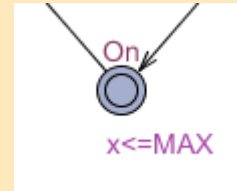


# Invariants

Scilab



Uppaal





Thanks!