



# Software Synthesis and Verification

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**Prof. Jüri Vain**

Tallinn University of Technology

# Why formal methods?

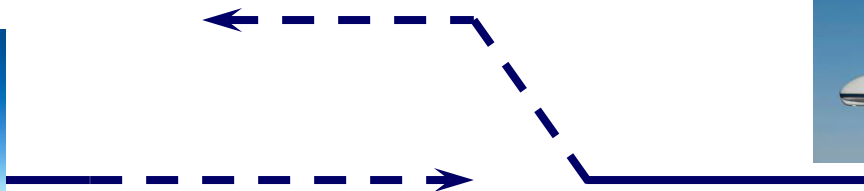
## Auto-pilot example

### Problem

Design a module for airplane auto-pilot that avoids collision with other airplanes.

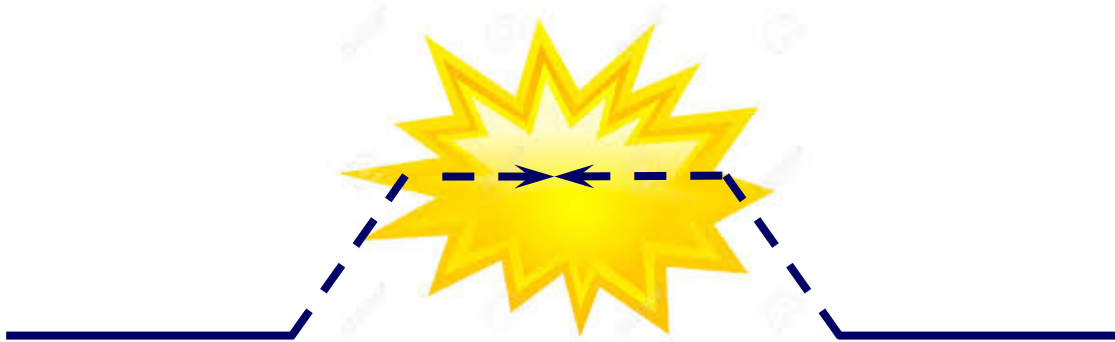
### Possible design solution (conceptually):

When distance is 3km, give warning to approaching plane and notify own pilot. When distance is 1km, and no course change is taken, go up.



# Problem with (bad) solutions

- Assume both planes have the same collision avoidance software. Then both go up and ...

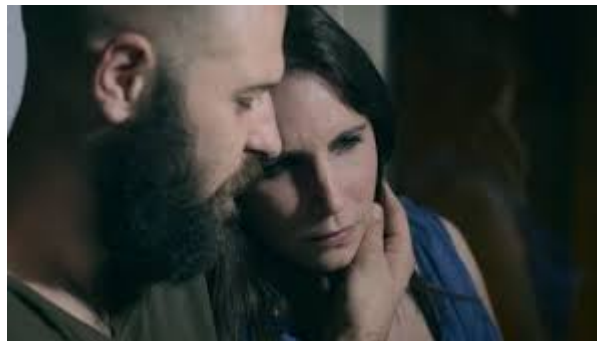


# This happens in real software!

- Some famous bugs
  - Several NASA space missions have been lost
  - Intel floating point processor bug
  - A military aircraft flipped when crossing the equator.
  - Bug in US F-16 software: aircraft control lost when flying low over Dead Sea (altitude < normal sea level)



# What makes CPS design so hard?



# Common characteristic of CPS: Complexity & Heterogeneity

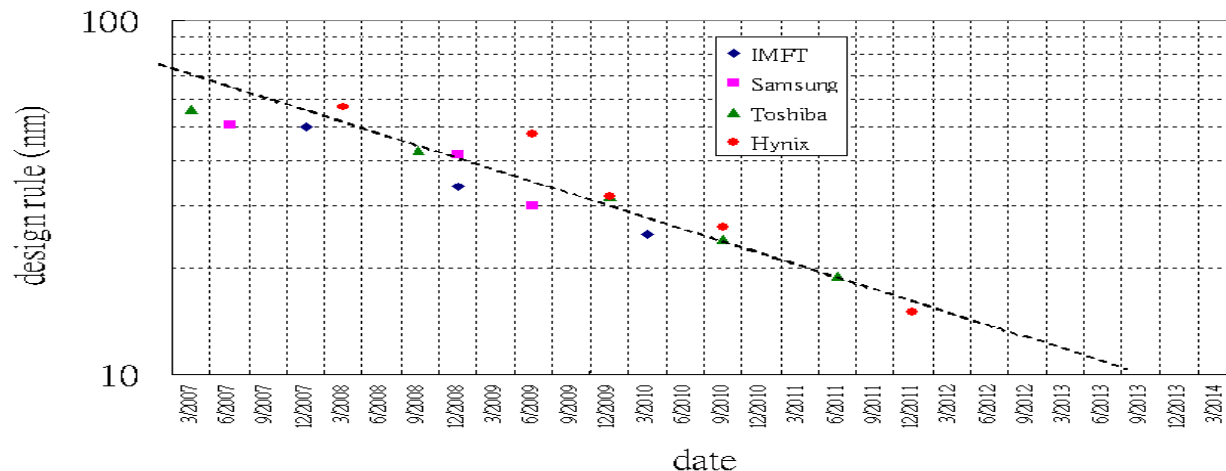
- **Multi-scale** technology integration and mapping that:
  - data gathering from simple sensors ... data warehouses;
  - data, computing, and services are **distributed** in the cloud;
  - access to data and services via various end-user utilities.
- The architecture is **open** and **dynamic** with
  - heterogeneous networking and
  - heterogeneous components.
- High level of **concurrency** with **complex interactions** where
  - the **location** of data&computation
  - and **timing** is critical



# Increasing performance of core technologies

## *Moore's Law:*

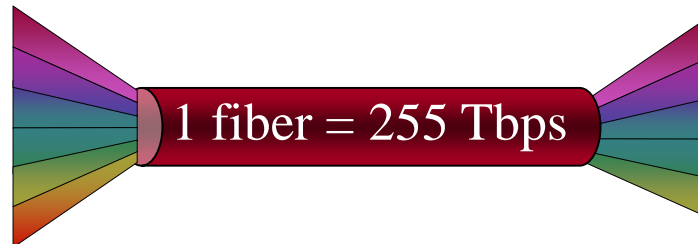
The performance of microprocessors doubles every 18 months



*Proebsting's law:* Compiler technology doubles the performance of programs every 18 years

# Increasing performance of core technologies

- *Gilder's Telecom Law:*
  - 3x bandwidth/year for 25 more years
- in 1996: whole US WAN bisection bandwidth was 1 Tbps
- in 2014:
  - TUE and U. of Central Florida have achieved **255 terabits** per second per optical fiber, i.e. 5.1 terabits per carrier





# Increasing dependability requirements

- Dependability is systems' and services' integral measure that captures
  - availability
  - reliability
  - maintainability
  - durability
  - safety
  - security
  - ...



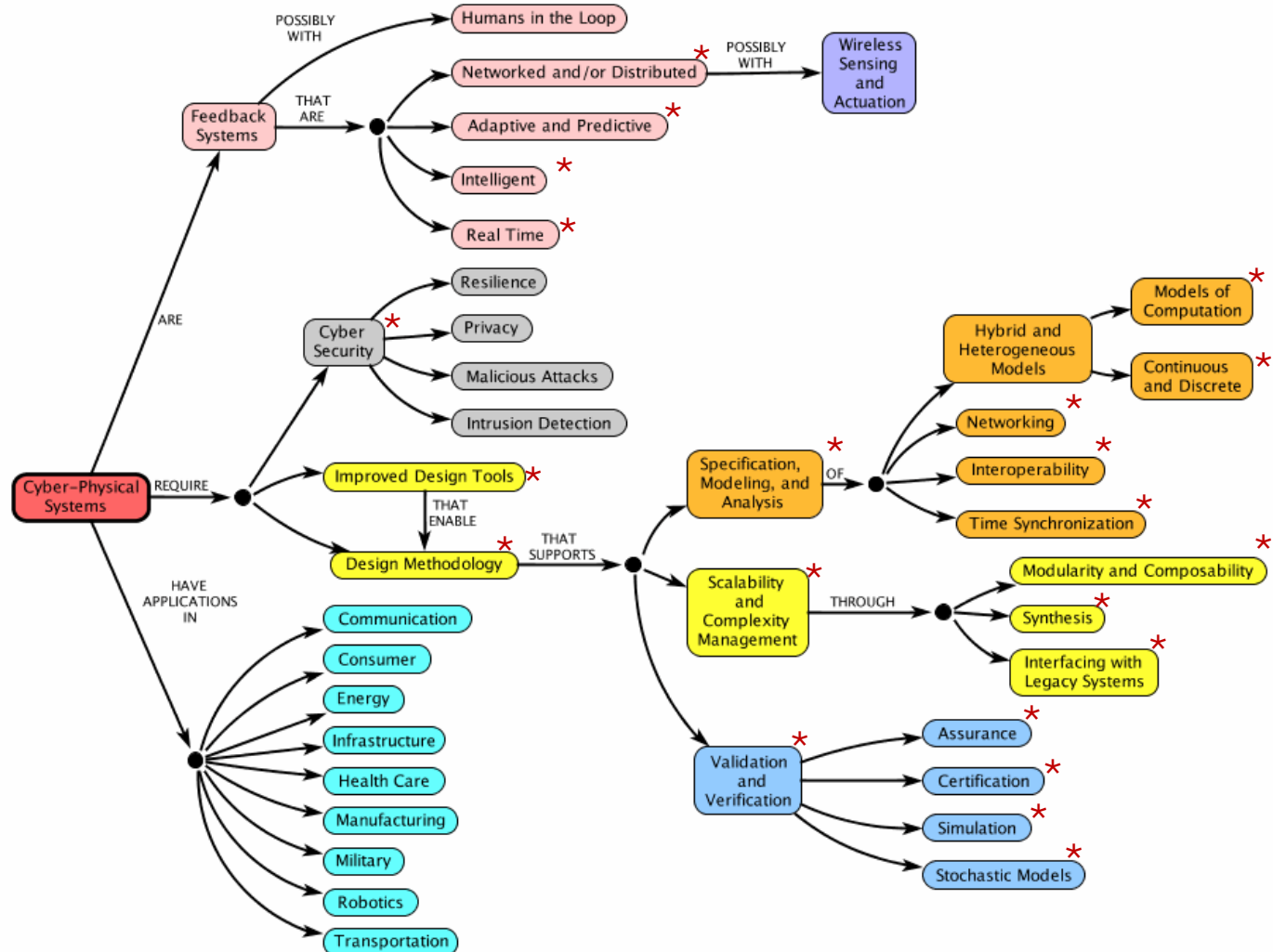
Ariane 5 accident

The launch failure brought the risks of complex systems to the attention of general public. The subsequent automated analysis of the Ariane code was the first example of large-scale [static code analysis](#) by [abstract interpretation](#). This led to the discipline of dependability for \* - [critical systems](#).

# Cyber-Physical Systems

## Cyber-Physical Systems – a Concept Map

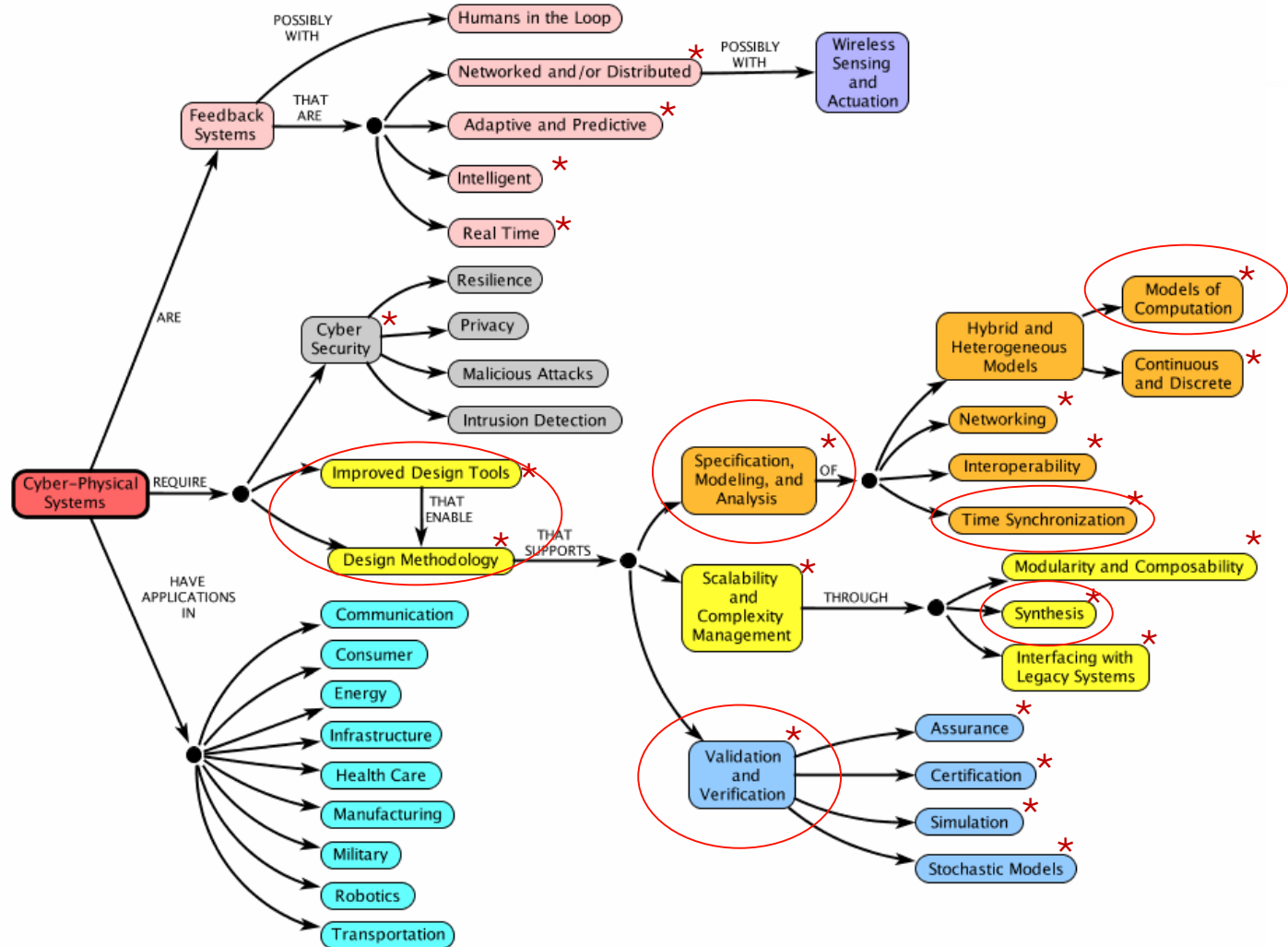
<http://CyberPhysicalSystems.org>



# Cyber-Physical Systems

## Cyber-Physical Systems – a Concept Map

<http://CyberPhysicalSystems.org>



# Implications of complexity & dependability for CPS development process

- Quality dilemma: drop the quality for more features
- Test and verification are the bottlenecks in design processes
- Error detection/diagnosis/repairment constitute 50-70% of costs

| Design task                               | Tasks delayed (%) |             |         | Tasks causing delay (%) |             |         |
|---|-------------------|-------------|---------|-------------------------|-------------|---------|
|   | Auto-motive       | Auto-mation | Medical | Auto-motive             | Auto-mation | Medical |
| System integration<br>T & V               | 63                | 56,5        | 66,7    | 42,3                    | 19          | 37,5    |
| System Archi-ecture<br>D&S                | 29,6              | 26,1        | 33,3    | 38,5                    | 42,9        | 31,3    |
| SW application and/or<br>middleware D & T | 44,4              | 30,4        | 75      | 26,9                    | 31          | 25      |
| Project management &<br>planning          | 37                | 28,3        | 16,7    | 53,8                    | 38,1        | 37,5    |

Source: Inria research report n° 8147 november 2012



# CPS design challenges (I): heterogeneity of requirements

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- Technology integration and mapping,
- Reliability and resilience,
- Power and energy consumption,
- Security,
- Diagnostics,
- Run-time management,
- Real-time feedback,
- ....



# CPS design challenges (II): Complexity

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- Strong dependency between design aspects (functionality, safety, security, ...)
  - how to assure the coherence of aspects?
- Variety of control/communication/coordination scales from minuscule pace makers to national power-grids
  - how the time scales match?
- High level of concurrency with complex interactions
  - how to explore the full state space?
- Wide spectrum of timing requirements of interacting components.
  - is design feasible regarding timing constraints



# How can formal methods/tools address CPS design challenges?

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FM must support

- Model-based development with rigorous formal semantic basis.
- Scalability and extendability of methods and tools.
- Compliance with state-of-the-art programming technologies and standards.
- Simplicity of use in industrial engineering.



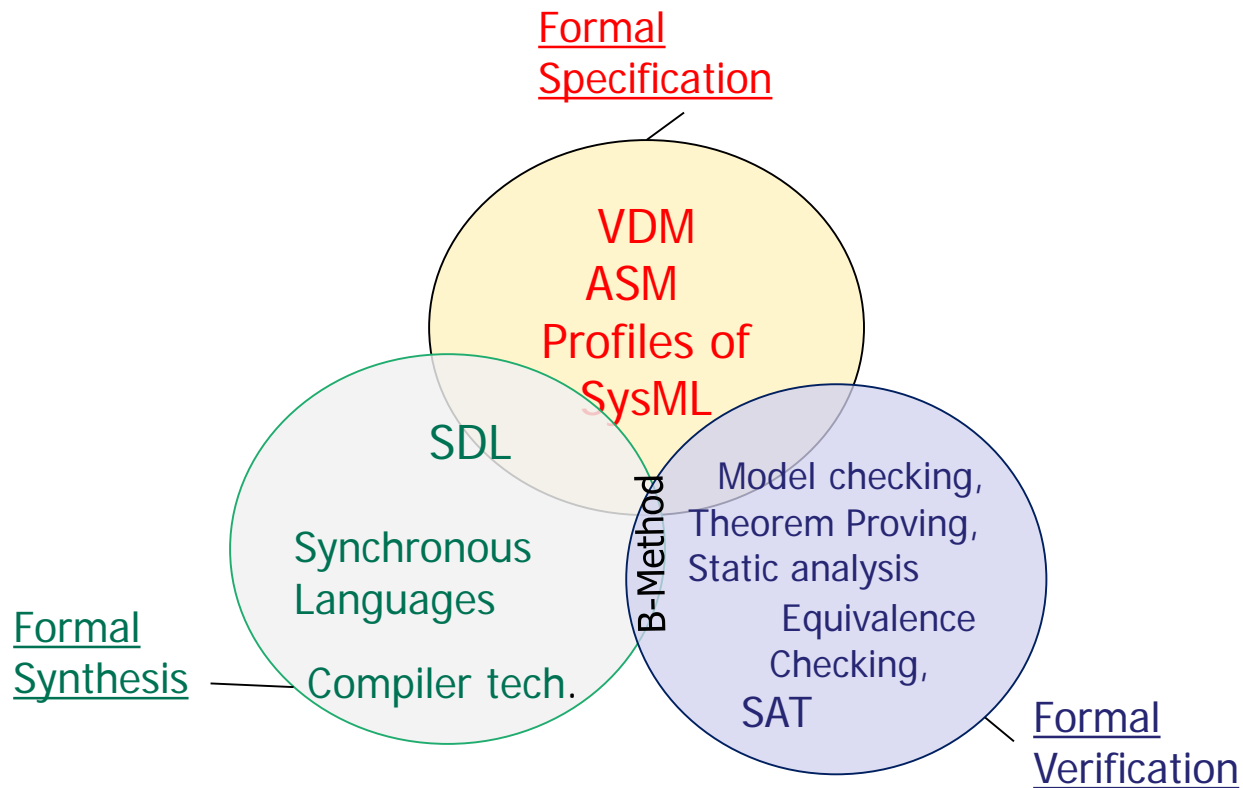
# Formal methods in a nutshell

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- FMs deal with formal notation – *state, data type, refinement,...*
- Formal notation has rigorous semantics
- FMs emphasize
  - symbolic reasoning
  - transformations
  - analysisof *abstract formal notations*.
- FMs is not esoteric science,  
e.g. compilation in a broad sense is a FM: high-level notation is transformed to low-level executable notation.



# Taxonomy of formal methods





# Formal Specification (1)

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- Given:
  - *possibly unstructured, fragmented, incomplete, ... descriptions of the system or its requirements expressed in different informal forms of representation.*
- Goal:
  - *express this knowledge about the structure, behavior, properties in some formal language.*



# Formal Specification (2)

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- abstracts from unnecessary implementation details
- provides rigorous mathematical semantics
- abstraction allows high-level reasoning while implementation details are not clear yet
- allows to avoid ambiguous or inconsistent specifications.

## Challenges:

- Specification refinement/ consistency checks/ aspect extraction are difficult to comprehend by engineers without theoretical training.
- Elaboration of domain oriented languages and their mapping to standard formalisms is required



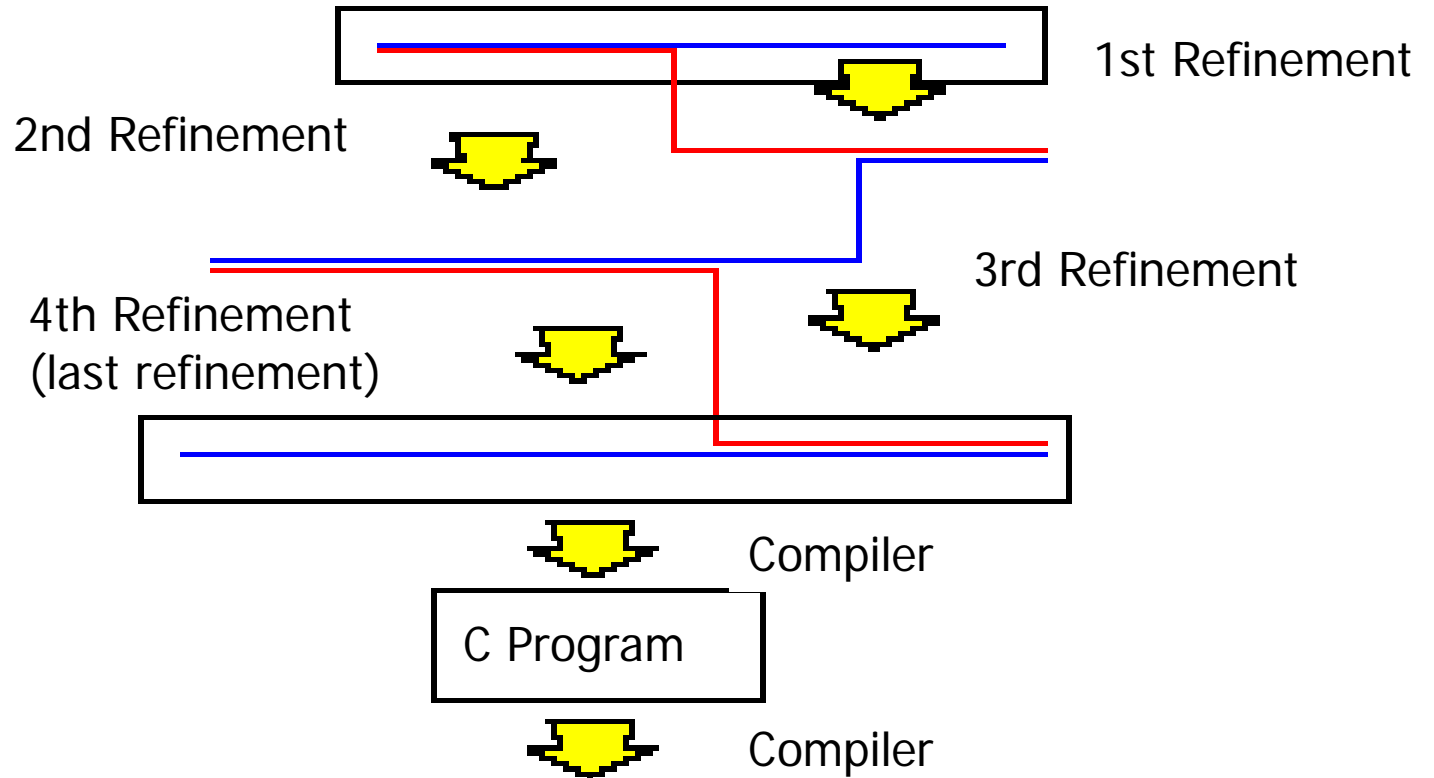
# Formal Synthesis (I)

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- Given:
  - Requirements to the artefact to be synthesised
  - (Possibly) design templates, patterns..., components
  - Design constraints (structure, behavior, properties,...)
  - Other constraints (cost, ethical, aesthetic, ...)
- Goal:
  - Construct architecture, control structure, data, code

# Refinement based Synthesis (I)

Requirements Specification





# Refinement based synthesis (II)

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- Integrates the refinement steps with verification.
- Incremental refinement steps are guided by **domain heuristics**.
- Refinement correctness verification is based on components' specifications and their composition rules i.e. **compositionality**.
- Proofs can be automatized but are **computationally expensive**.
- Refinement steps may be either
  - correct by construction or
  - *'invent-and-verify'*.
- Example: B-Method and Rodin tool (Event-B.org)





# Formal Verification

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Given: system requirements specification and implementation

Prove: that implementation *satisfies* the requirements specification

- Full blown “post mortem verification” is too complex
- Simplifications applied are:
  - partial specifications (slicing, aspect orientation, contracts):
    - type safety,
    - functional equivalence of systems,...
  - compositionality (deduce the correctness of whole from the correctness of components);
  - property preserving abstractions, and reduction techniques.



# Classes of verification methods

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- Boolean methods:
  - SAT, BDDs, ATPG, combinational equivalence check
- Finite state methods:
  - bisimulation and equivalence checking of automata, model checking (MC)
- Term based methods:
  - term rewriting, resolution, tableaux, theorem proving
- Abstraction based methods
  - BDDs, symbolic MC, theorem proving, SMT constraint solving





# Software Oriented Formal Methods

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- Model-based testing (MBT)
- Deductive verification
- Model checking (automatic verification)
- Static analysis
- SMT- constraint solving
- Combinations of the above

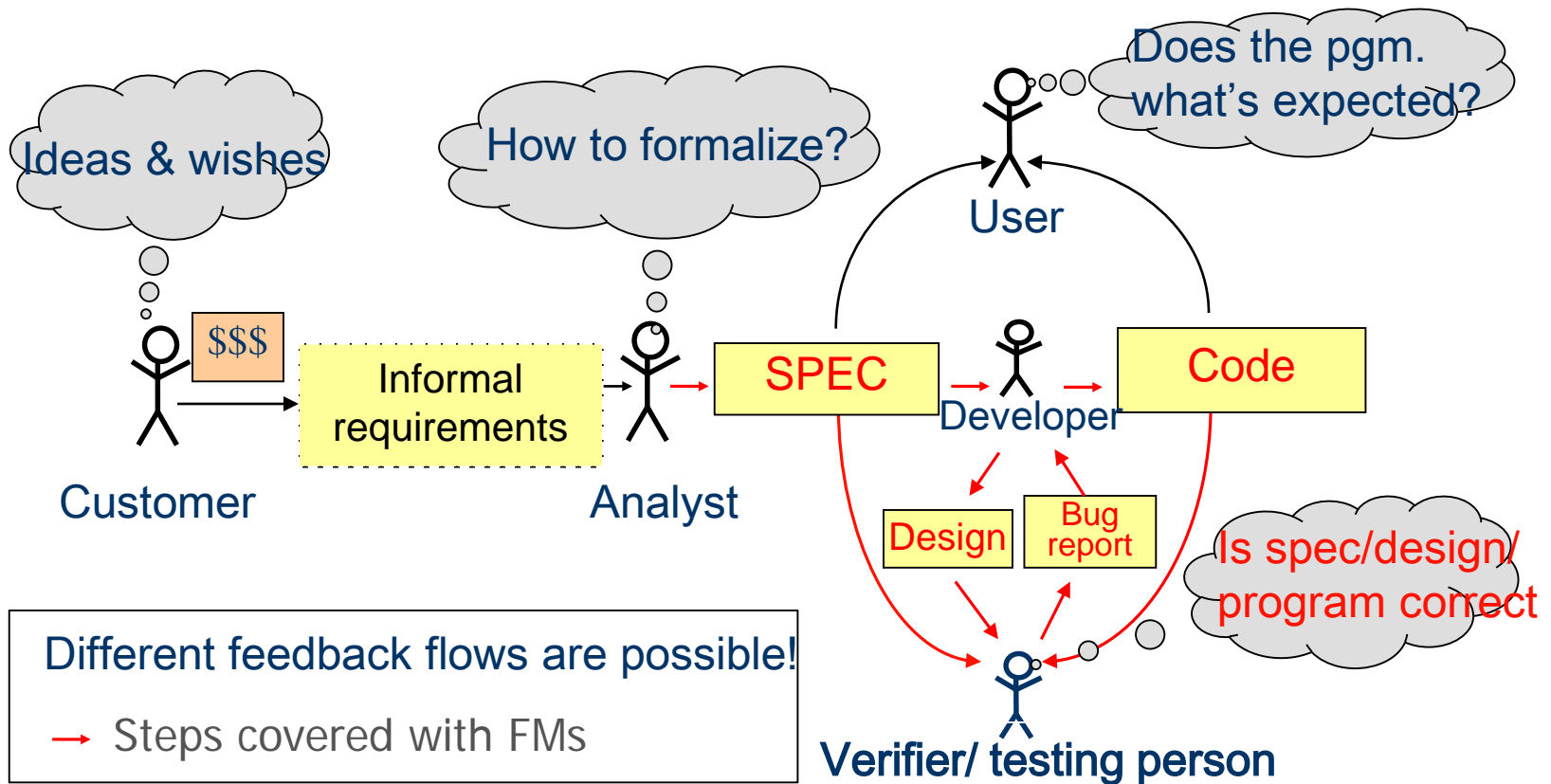


# Test & Verification

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- **Testing**
  - dynamic execution / simulation of system runs
  - *Present view*: tests have to be integrated in the development process
  - *Extreme view*: testing should “drive” the development process
- **Verification**
  - *Means*: static checking, symbolic execution.
  - In HW design community: verification means also testing
- **In FM community Testing ≠ Verification**
  - Testing is *partial* exploration method (not all executions are covered)
  - Verification is *complete* method but more costly than testing

# Verification: process and parties



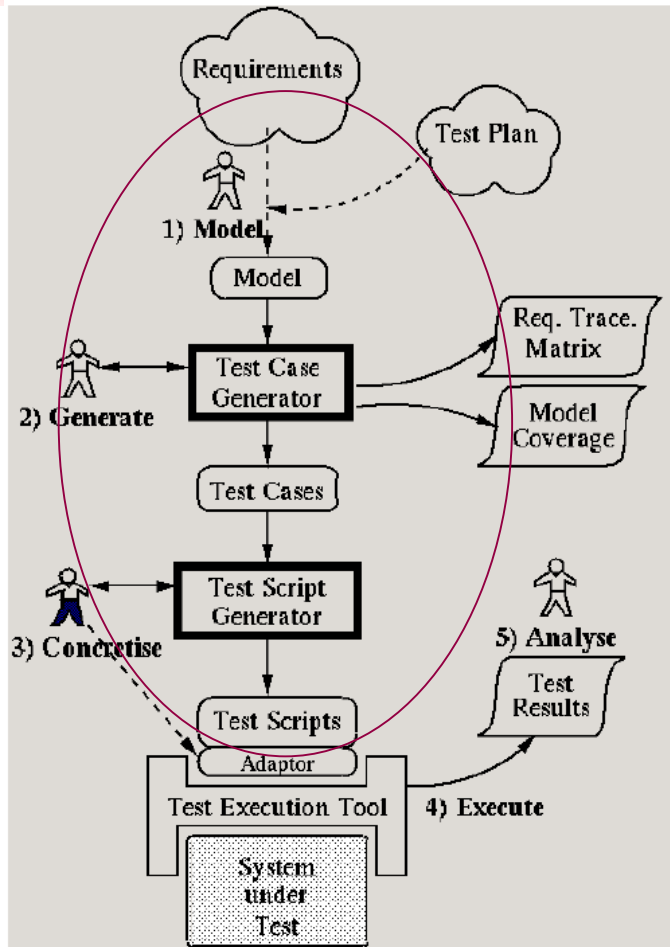


# (Traditional) testing

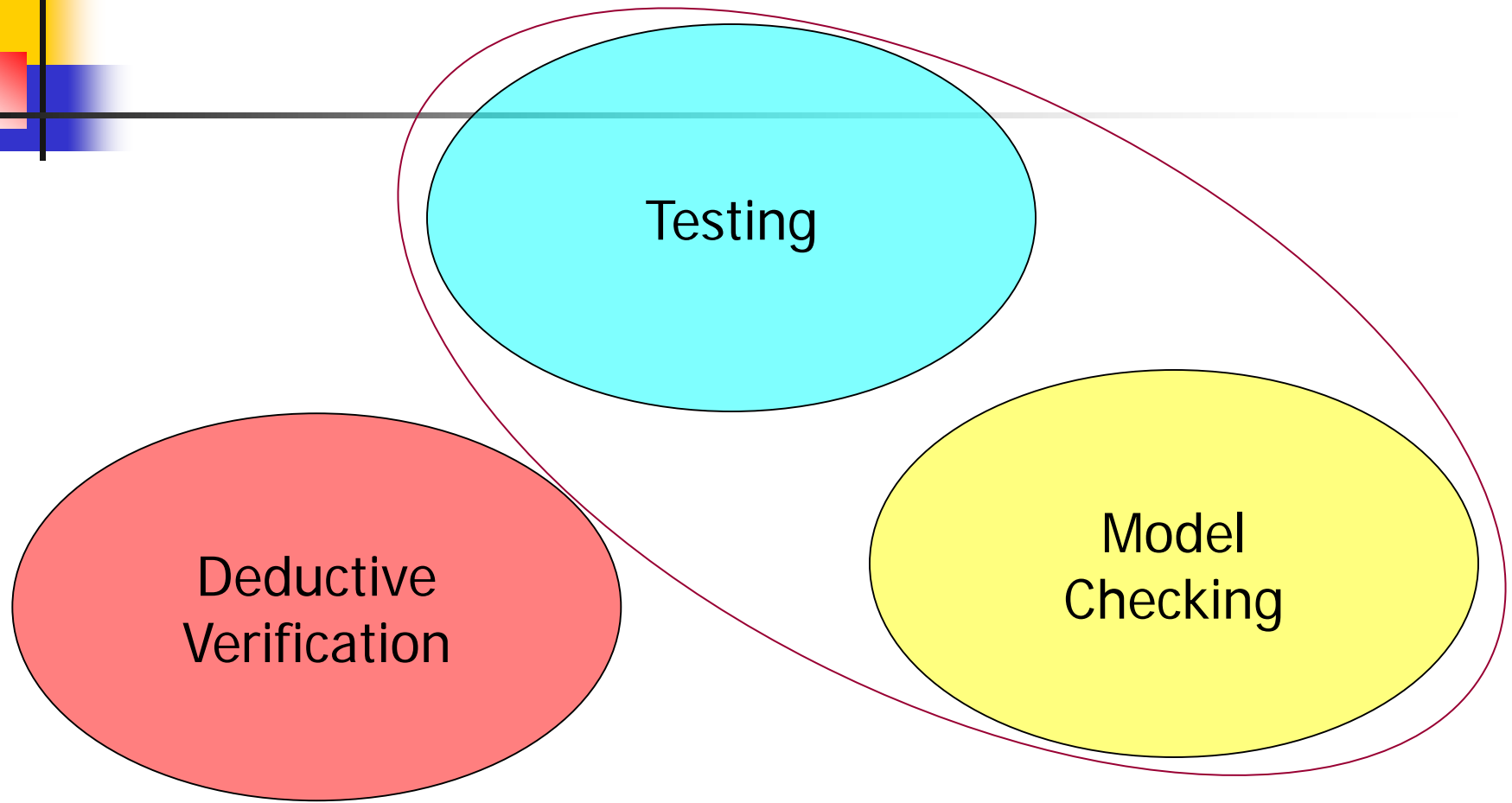
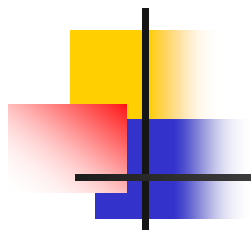
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- Executing the software in order to exercise and discover errors
- Still most handy and common method in sw industry +
- Partially manual, some automation tools exist (for running tests, organizing test data and reporting) -
- Applicable directly on executable software +
- Not exhaustive, errors often survive -
- Depends on tester's intuition and experience +/-
- Formal spec is not needed +/-

# Model-Based Testing (MBT)



- **Goal:** Check if real system conforms with requirements specification.
  - **Advantages/disadvantages**
    - + model hides irrelevant details of implementation;
    - + automatic generation and execution of tests;
    - + systematic coverage of requirements
    - + relevant for **regression testing**
- modeling overhead!





# Model Checking

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Given a model  $M$  and a property  $P$ , check if  $M$  satisfies  $P$

- **Exhaustive** state space exploration method.
- Uses graph theory and automata theory to decide on properties of programs **algorithmically**
- **State space explosion**: complexity of the problem or bad modeling causes exponential memory and time growth
- Due to algorithmic state space exploration the method is limited, suites for **finite state** systems
- But there are many heuristics and techniques to reduce time and memory space



# Deductive Verification

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Applies *theories* and *logic inference* to prove properties of system **specification** formally

- Is based on proof theory and techniques +
- When doable provides *full certainty* of correctness +
- Requires expertise in logic, math and tools usage -
- Highly time consuming (inertive) -
- Susceptible to discrepancies between sw and model -
- Practical only with tool support -
- Applicable on small and medium size examples -
- Requires accurate specification -

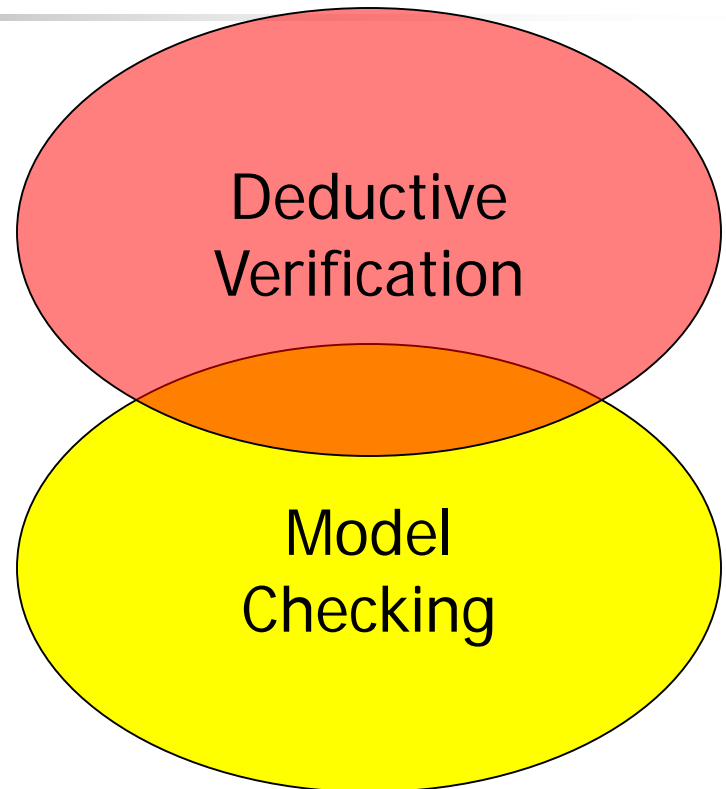


# Comparing verification methods

| Method \ Criterion         | Testing                         | Deductive Verification               | Model Checking                    |
|----------------------------|---------------------------------|--------------------------------------|-----------------------------------|
| Size of system             | Small-Very large                | Limited examples                     | 100s-1000s lines                  |
| Time                       | Minutes-Hours                   | Days-Weeks                           | Minutes-Hours                     |
| Expertise needed           | Test engineers/<br>programmers  | Mathematicians,<br>Comp-Sci., Logic. | Comp.-Scientists/<br>sw engineers |
| Popularity                 | SW/HW industry                  | Mostly research                      | Reserch/industry                  |
| Specification              | Informal<br>requirement docs    | Logic or<br>automata based           | Logic or<br>automata based        |
| Modelling /<br>corrections | Not needed /<br>code correction | Must /via formal<br>representation   | Must/via formal<br>representation |

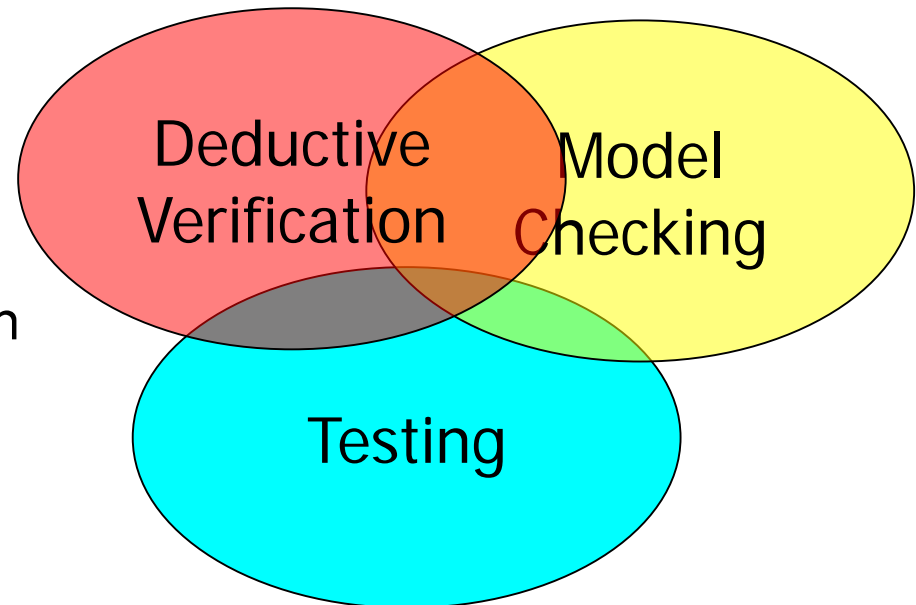
# Integrated FM (I): Symbolic model checking

- General strategy
  - Find symbolic states and transitions by proving equivalences of explicit states.
  - Then apply model checking on this finite abstractions.



# Integrating formal methods (II): Symbolic Verification / Testing

- Apply **abstraction** techniques to generate symbolic states and transitions of the system model.
- Apply **symbolic model checking** to generate abstract witness traces for temporal formulas that describe the test goals.
- Apply these witness traces as **test sequences** instantiated with concrete test data.

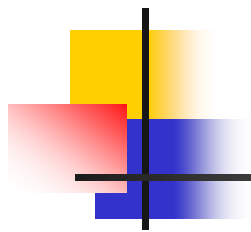




# Instead of summary: Current trends of FM

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- Trying to solve special cases of generally undecidable or highly complex problems.
- Improving usability
- Integrating mutually complementing FMs
- Building industry strength aka scalable tools
- Applying parallelization, distributed and high-performance computing
- Combing FM with AI and soft computing techniques.



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Questions?